A Comparison of Flow Rates and Pressure Profiles for N-Sequential Inlets and Three Related Seal Configurations

R. C. Hendricks

Lewis Research Center

Cleveland, Ohio

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R.C. Hendricks

National Aeronautics and Space Administration Lewis Research Center Cleveland Ohio 44135

INTRODUCTION

In general, dynamic seals can be categorized into four basic types, shaft, face, labyrinth, blade tip or their combinations. The flow field for the shaft or cylindrical seal is simplest to describe and the tip seal is the most complex due to a combination of axial flow around the blade and circumferential flow over the tip.

In analyzing a seal, three fundamental characteristics are important: (i) the leak rate and associated pressure profile; (ii) the response of the flow field to eccentric positioning of the centerbody, which provides seal stiffness and dampening essential to turbomachine stability and; (iii) applicability of a given result to other working fluids.

Critical mass flux or leak rates were determined in Refs. 2 to 4, and pressure signatures were established for flow through simulated turbopump cylindrical, stepped cylindrical and labyrinth shaft seals. Concentric and fully eccentric (to point of rub) positions were examined. The data were taken with fluid nitrogen and hydrogen. In general it was found that the mass flux or leak rate, for each configuration could be normalized using the principles of corresponding states and the theory of two-phase-choked flows. The presssure profiles, however, did not show any direct correspondence 5-8 as explained in Refs. 7 and 8.

Many seals effectively have multiple inlets. Labyrinth seals are good examples of this. In Refs. 9 and 10, flow rate and axial pressure profile data for fluid nitrogen are presented for 20, 15, 10, and 7 N-sequential orifice-inlet configurations uniformly spaced at 15.5 cm. These data were correlated over a wide range in reduced inlet stagnation temperature (from 0.7 to ambient) and reduced inlet stagnation pressure (up to 2) and are in general agreement with previous studies of one to four inlets. Experimental and theoretical agreement for liquid and gas flow data was acceptable but inconclusive in the near thermo-dynamic critical regions. The objective of this paper is to compare normalized leakages (flow rates) and pressure profiles for the three seal geometries of Refs. 2, 4, 7, and 11 with those of the classic venturi Refs. 5 and 6 and the N-sequential orifice configuration to provide a relative measure of seal effectiveness Refs. 8 to 10.

SYMBOLS

```
mass flux
     normalized mass flux, \sqrt{P_{c\rho}/Z_c}, 6010 g/cm<sup>2</sup>-s for
G*
       nitrogen
     local axial position
L
     total axial position
     number of sequential orifices
N
P
     pressure
Т
     temperature
Z
     compressibility
     density
Subscripts
     thermodynamic critical
j,k
     indices
     stagnation
     reduced or normalized
```

GEOMETRIC CONFIGURATIONS

Figure 1a shows the straight cylindrical seal where the centerbody diameter is 8.4244 cm and the seal length is 4.13 cm with a clearance of 0.0135 cm. Figure 1b shows the three step cylindrical seal. In general, the clearance is 0.0127 cm with a 0.038 to 0.051 cm slot spacing between shaft shoulder and the housing at each step and a total length of 4.62 cm. The shaft diameters were 7.9233 cm, 7.8346 cm, and 7.6944 cm, respectively, decreasing in the direction of flow. Figure 1c shows two of the three step labyrinth type seals with 12, 11, 10 teeth per step at nominal diameters of 8.077 cm, 7.976 cm, and 7.874 cm, respectively, in the direction of flow with an overall length of 4.38 cm.

Figure 1d illustrates the N-inlet test configurations. The orifices, 0.478 cm diameter with 1/D of 0.5, were spaced at 32 orifice-diameters or approximately 15.5 cm aperture to aperture.

RESULTS AND DISCUSSION

Choked Flow Rate

From the conservation equations, choked flow and normalizing parameters can be determined which can be used to correlate data for a variety of fluids. 5,6 Further, the N-sequential orifice configuration can also be solved using a modified form of these techniques where the governing equations are solved at each orifice assuming the carryover (jet kinetic energy or fluid recovery due to incomplete expansion) to be small, and iterated to a solution. 10 Although many theoretical calculations have been made to relate the flow rates in the various geometries, the methods are complex and described in Refs. 5, 6, 10 and will not be repeated herein. In all cases the mass flux, G_r (i.e., leakage rate), data were correlated using the normalizing parameter G*

$$G_{r} = \frac{G}{G^{*}} \tag{1}$$

as a function of reduced inlet stagnation pressure and inlet stagnation temperature:

$$P_{r,o} = \frac{P_o}{P_c}$$

$$T_{r,o} = \frac{T_{r,o}}{T_c}$$
(2)

either a constant or in general a parameter. The normalizing parameters relating mass flux, G*, P_C, and T_C are only dependent on the properties of the working fluid at the thermodynamic critical point. These corresponding states parameters have been used to correlate large sets of data for a variety of simple fluids and are applied to the nitrogen data for the seal and N-sequential orifice configurations.

Figure 2a presents the reduced flow rates at $T_{r,0} = 0.7$ as a function of reduced inlet stagnation presssure for the venturi, the three seal configurations and N-sequential orifices. The values for N = 33 were obtained by extrapolating the data and using the analytical treatment presented in Ref. 10. On a relative basis, one can say that the cylindrical seal behaves

much like a sharp edge orifice i.e., $0.6 \times G_r$, venturi $(0.5 \times G_r)$, theory). The three step seal provides approximately 1/3 less leakage $(0.7 \times G_r)$, cylindrical) and the labyrinth seal provides about 1/5 less leakage $(0.8 \times G_r)$, 3-step). The 33-sequential orifices seal has about 1/2 the leakage of the 33-tooth labyrinth seal $(0.5 \times G_r)$, 33-tooth labyrinth), which is indicative of carryover in the seal. Further, these results for mass flux, leakage, are not significantly influenced by eccentricity.

Figure 2b presents the reduced flow rates at $T_{r,o}=2.2$ (ambient gas) for the same geometries of Fig. 2a. Again on a relative basis, one can say that the cylindrical seal behaves somewhat like an orifice i.e., 0.7 x G_r , venturi. The three step seal provides approximately 1/3 less leakage (0.7 x G_r , cylindrical) and the labyrinth seal provides about 1/3 less leakage (0.7 x G_r , 3-step). The 33-sequential orifices has about 1/2 the leakage of the 33-tooth labyrinth seal (0.5 x G_r , 33-tooth labyrinth), again indicating the influence of carryover in the seal. These results do not appear to be significantly influenced by eccentricity or small convergent taper. 11

Pressure Profiles

In Fig. 3, the axial pressure profiles are normalized in terms of the inlet stagnation pressure and plotted as a function of normalized length (ℓ/L). The normalized length for N-squential inlets can be expressed as the number of orifices up to 1 (i.e., Σ N_j) to the length to choke L (i.e., Σ N_k), where k \geq j. 10

In Fig. 3a, the normalized pressure profiles for the seal geometries and N-sequential inlets are linear with normalized length for $T_{r,o}=0.7$. This is significant because the geometries are very different yet when properly normalized they appear similar. These profiles indicate a universality between geometries for a designer knowing the inlet stagnation and choke condition, the pressure profile is then known. The pressure profiles are very important to turbomachine stability because there are usually several sealing surfaces between bearing supports. 1

SUMMARY

Studies of experimental and analytic results have been carried out to determine the effectiveness of labyrinth, 3-step, and cylindrical type shaft seal configurations. Similar studies have also been carried out for N-sequential orifice type inlets.

The flow rates and pressure profiles were calculated based on a two-phase choked flow approach and modified for the labyrinth seal and sequential inlet geometries. For the N-sequential inlet configuration, the carryover (jet kinetic energy not dissipated during expansion) was assumed to be small and the solution required an iterative procedure. All data were normalized in terms of the parameters, G*, P_C, and T_C which depend only on fluid properties at the thermodynamic critical point.

The flow rates, or seal leakages, are significantly influenced by the geometric configuration and fluid state. On the average, the cylindrical seal leakage is about 60 percent that of a venturi; the 3-step is about 70 percent of the cylindrical seal; the 33-tooth labyrinth is about 75-80 percent of the 3-step seal; and the 33-sequential orifice inlet configuration is about 50 percent of the 33-tooth seal. The implication for the latter two geometries is that carryover can represent a significant part of the leakage.

The normalized pressure profiles are less distinctive, but most important to seal dynamics. In general these profiles are linear for liquid flows with little effect due to geometry. However separation effects observed in the 3-step seal are nonlinear and could profoundly alter turbomachine dynamics. Such a profile is common to eccentric placement of the shaft-housing configuration (i.e., to the point of rubbing). The normalized pressure profiles gaseous operation are parabolic and are more sensitive to geometric changes. Such normalized profiles suggest universality and are readily adapted to design methodology. More work will be required to establish these concepts.

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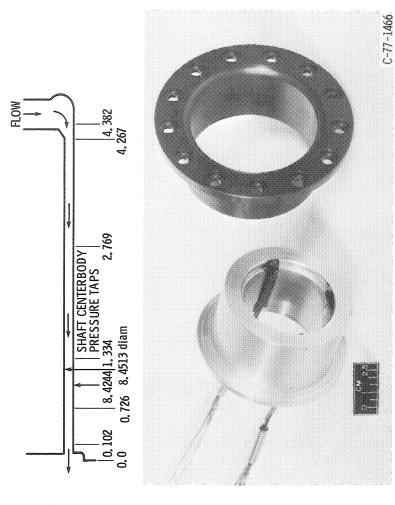


FIGURE 1a. - CYLINDRICAL SHAFT SEAL.

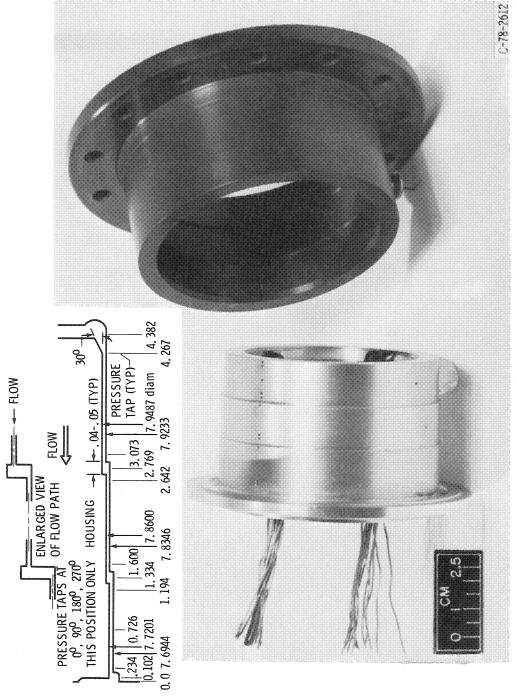


FIGURE 1b. - 3-STEP SHAFT SEAL.

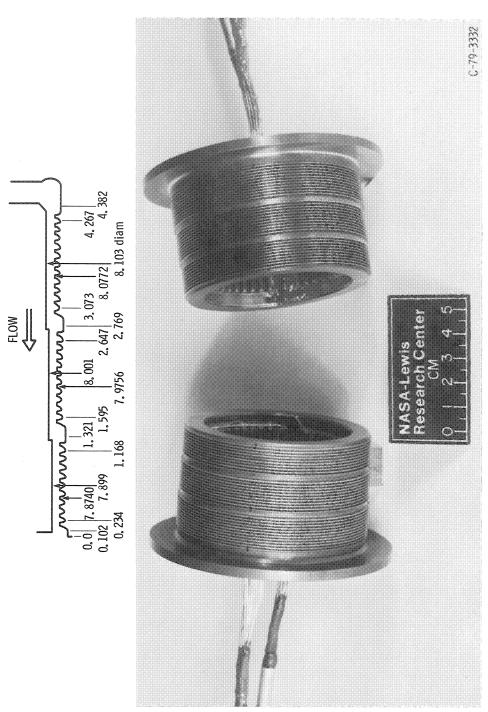


FIGURE 1c. - 33-TOOTH LABYRINTH SHAFT SEAL.

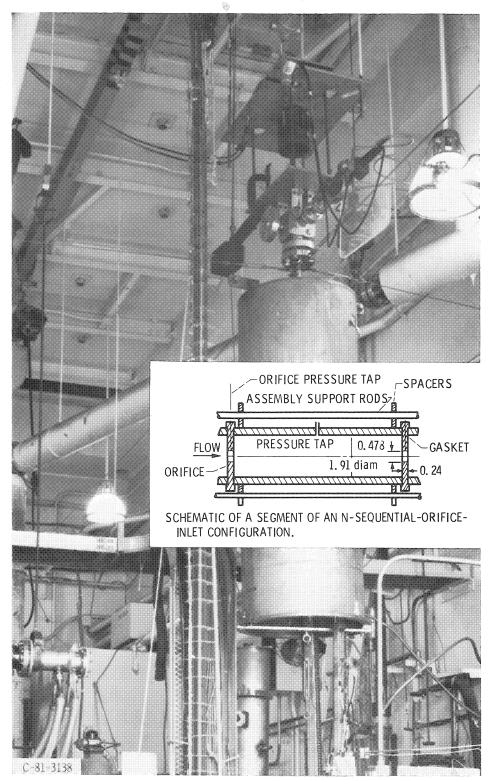


FIGURE 1d. - N-SEQUENTIAL ORIFICES.

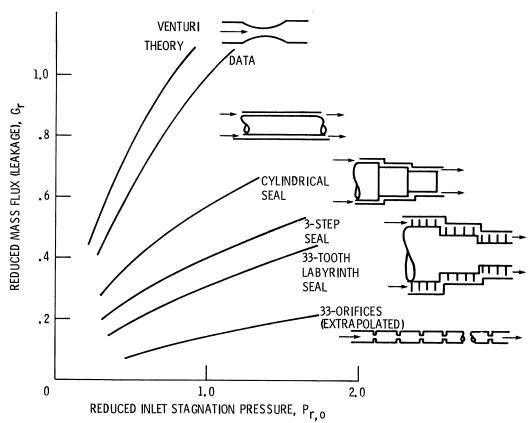


FIGURE 2a. - REDUCED MASS FLUX (LEAKAGE RATES) AS A FUNCTION OF REDUCED INLET STAGNATION PRESSURE WITH REDUCED INLET STAGNATION TEMPERATURE OF 0.7 FOR FIVE GEOMETRIC CONFIGURATIONS; VENTURI, CYLINDRICAL SEAL, 3-STEP, 33-TOOTH LAYBYRINTH, AND N-SEQUENTIAL ORIFICES.

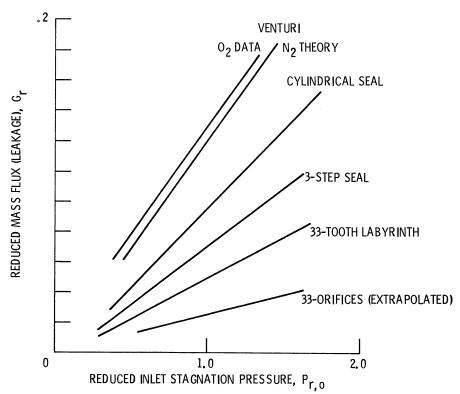
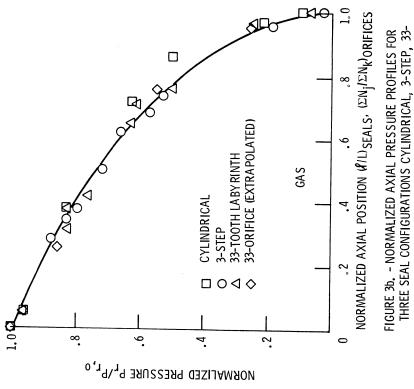
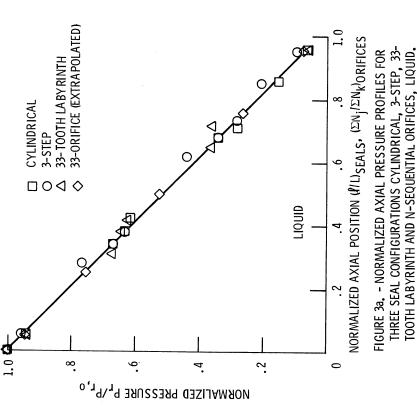


FIGURE 2b. - REDUCED MASS FLUX (LEAKAGE RATES) AS A FUNCTION OF REDUCED INLET PRESSURE WITH INLET STAGNATION TEMPERATURE AT AMBIENT GAS FOR FIVE GEOMETRIC CONFIGURATIONS VENTURI, CYLINDRICAL SEAL, 3-STEP, 33-TOOTH LABYRINTH, AND N-SEQUENTIAL ORIFICES.



TOOTH LABYRINTH AND N-SEQUENTIAL ORIFICES, GAS.



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